CHAPTER 17 CHEMICAL EQUILIBRIUM

Dr. Floyd Beckford Department of Chemistry Texas A&M University © Spring 1998 • Reactions that do not go to completion are called reversible reactions

• Chemical equilibrium: exists when two opposing reactions occur simultaneously at the same rate

• *Dynamic* equilibrium: overall concentrations of species is constant but reactions does not stop

THE EQUILIBRIUM CONSTANT, K

• At equilibrium, [reactants] is not necessarily equal to [products]

• Relationship between concentrations of

reactants and products is called the equilibrium

constant expression

Reactants
$$\underset{k_r}{\overset{k_f}{\longleftarrow}}$$
 Products

- For the forward reaction; rate = k_f[products]
- For the reverse reaction; rate = k_r[reactants]
- At equilibrium, k_f[products] = k_r[reactants] k_f/k_r = [Products]/[Reactants]
- \bullet The ratio $k_{\rm f}/k_{\rm r}$ is called the equilibrium constant, $K_{\rm c}$

K_c = [**Products**]/[**Reactants**]

• For the general reaction

$$aA + bB \rightarrow cC + dD$$

$$\mathbf{K}_{\mathbf{c}} = \frac{\left[\mathbf{C}\right]^{\mathbf{c}} \left[\mathbf{D}\right]^{\mathbf{d}}}{\left[\mathbf{A}\right]^{\mathbf{a}} \left[\mathbf{B}\right]^{\mathbf{b}}}$$

 $Fe^{3+}(aq) + 2SCN(aq) \rightarrow Fe(SCN)_2^+(aq)$

.

$$\mathbf{K}_{\mathbf{c}} = \frac{[\mathrm{Fe}(\mathrm{SCN})_2^+]}{[\mathrm{Fe}^{3+}][\mathrm{SCN}^-]^2}$$

• In discussing K_c activities are used in preference to concentrations

• The activity of a compound is the ratio of its concentration (or partial pressure) to a standard concentration (1 M or 1 atm)

• The values used to calculate the equilibrium constant are numerically equal to concentration but has no units

•The equilibrium constant has no units

• For activities

1. For *pure* liquids and solids, the activity is taken as **1**

2. For components in an ideal solution, the

activity of each component is taken to be equal to its molar concentration

3. For gases, activity equals the partial pressure

For K_c

- The numerical value of K_c indicates the extent to which the reaction has proceed
- Can be used to predict if a reaction is productor reactant-favored
- The value varies with only with temperature
- It is constant at a given temperature
- It is independent of the initial concentration

 \bullet The larger the value of $K_{c}~(K_{c}>1)$ the more product-favored is the reaction

 \bullet The smaller the value of $K_{\rm c}~(K_{\rm c}<\!\!<\!\!1)$ indicates the reaction does not proceed to any extent

• The reaction is reactant-favored

 $PbI_{2}(s) = Pb^{2+}(aq) + 2I(aq)$ $K_{c} = [Pb^{2+}][I^{-}]^{2}$

• Recall activity of solids and solvents is 1

 \bullet They are not involved in the $K_{\rm c}$ expression

Variation of K_c

• The equilibrium constants for a reaction and its reverse are reciprocals of each other

• When stoichiometric coefficients of a balanced equation are multiplied by some factor f, the equilibrium constant for the new equation (K_{new}) is the equilibrium constant for the old reaction

 (\mathbf{K}_{old}) raised to the power of the factor, f

• In general when two or more equations are added to produce a new equation, the equilibrium constant for the net equation is the product of the equilibrium constants for the added reactions •Q is used to determine direction the reaction has to move to reach equilibrium

- Q < K: Forward reaction predominates until equilibrium is reached
- Q = K: Equilibrium is established
- Q > K: Reverse reaction predominates until equilibrium is established

Factors affecting equilibrium

- Systems at equilibrium are governed by LeChateliers' Principle: If a change of conditions is applied to a system at equilibrium, the system responds in such a way as to reduce the effect of the change in attaining a new equilibrium
- The reaction quotient helps
- Four factors: concentration, temperature, volume and catalysis

1. Concentration

A + B → C • Addition of more reactants or products causes the system to shift the equilibrium in the direction that uses up the added species • Reactants added = Q < K. Forward reaction will dominate to re-establish equilibrium • Products added = Q > K. Reverse reaction will dominate to re-establish equilibrium

| Stress | Q | Shift of |
|-------------|-------|---|
| | | $\mathbf{A} + \mathbf{B} \leftrightarrow \mathbf{C} + \mathbf{D}$ |
| Increase in | Q < K | → right |
| [A] or [B] | | |
| Increase in | Q > K | ← left |
| [C] or [D] | | |
| Decrease in | Q > K | ← left |
| [A] or [B] | | |
| Decrease in | Q < K | \rightarrow right |
| [C] or [D] | | |

2. Pressure/Volume changes

• Important only for gas phase reactions

• A volume decrease (pressure increase) is counter-balanced by shifting the equilibrium position to the side with fewer gas molecules

• The reverse is true

• No change in the number of moles means volume (pressure) change does not affect the equilibrium position

3. <u>Temperature</u>

Generally,

- · Increasing in temperature moves the reaction in
- a direction that absorbs energy
- Decreasing in temperature moves the reaction in
- a direction that releases energy
- Depends on the type of reaction
- Temperature increase favors endothermic rxns
- Temperature decrease favors exothermic rxns

4. Catalyst

• Introduction of a catalyst has NO effect on the equilibrium position

• Equilibrium is established faster

•A catalyst only speeds up a reaction. Both forward and reverse reactions are affected equally

Pressure and the equilibrium constant

• For a gas phase reaction

$$\begin{split} \mathbf{P} &= (\mathbf{n}/\mathbf{V})\mathbf{RT} = \mathbf{MRT}\\ \mathbf{aA}(\mathbf{g}) + \mathbf{bB}(\mathbf{g}) \leftrightarrow \mathbf{cC}(\mathbf{g}) + \mathbf{dD}(\mathbf{g})\\ \mathbf{K}_{\mathbf{p}} &= (\mathbf{P}_{\mathbf{C}})^{\mathbf{c}}(\mathbf{P}_{\mathbf{D}})^{\mathbf{d}}/(\mathbf{P}_{\mathbf{A}})^{\mathbf{a}}(\mathbf{P}_{\mathbf{B}})^{\mathbf{b}} \end{split}$$

P_C, P_D, ... are partial pressures in atmospheres

• As with K_c, K_p has no units

 $\mathbf{K}_{c} = \mathbf{K}_{p}(\mathbf{RT})^{-\Delta n}$

$$\Delta \mathbf{n} = \mathbf{n}_{\text{gas prod}} - \mathbf{n}_{\text{gas react}}$$

Free energy and the equilibrium constant

- Standard free energy change is ΔG°
- \bullet For other concentrations free energy change is ΔG

 $\Delta \mathbf{G} = \Delta \mathbf{G}^{\mathbf{o}} + \mathbf{RT} \ln \mathbf{Q}$

At equilibrium, $\Delta G = 0$, and Q = K $0 = \Delta G^{\circ} + RT \ln K$ $\Delta G^{\circ} = -RT \ln K$ For ΔG° < 0, ln K >0, K > 1 : Products are favored over reaction (spontaneous reaction)
ΔG° > 0: Reactants are favored and reaction is nonspontaneous

- The magnitude of K relates directly to ΔG^o
- \bullet A very negative ΔG^o means K is large and the reaction goes to "completion"

Temperature - K_c relationship

• Equilibrium constants can be calculated at different temperatures from the van't Hoff equation

- Must know ΔH^o for the reaction

$\ln (K_1/K_2) = \Delta H^o/R(1/T_1 - 1/T_2)$

 K_1 = equilibrium constant at temperature T_1 K_1 = equilibrium constant at temperature T_1