

Chapter 2: Atoms, Molecules and Ions

The present picture of the atom has evolved over many hundreds of years. The history of the development of atomic theory is given in your textbook.

These are the 3 fundamental particles given in order of their discovery:

Particle	Mass	Charge	Discoverer
electron (e^-)	0.00055 amu	-1	Davy (1800's) + others
proton (p or p^+)	1.0073 amu	+1	Goldstein (1886)
neutron (n or n^0)	1.0087 amu	0	Chadwick (1932)

In 1910, the research group of Ernest Rutherford ran a most important experiment now called the Rutherford Scattering Experiment, in which a piece of thin gold foil was bombarded with alpha (α) particles (products of radioactive decay).

alpha particle \equiv He nucleus (atom minus its 2 electrons)
 ${}^4_2\text{He}^{2+}$ (it has a 2+ charge)

Most of the positively charged particles passed through the foil (that was expected); but some were deflected by the foil and a few bounced almost straight back. (Surprise!!) What did this mean? (Fig. 5-4, 5-5)

1. atoms are mostly empty space.
2. the mass of an atom is located primarily in the nucleus at the center of the atom.
3. the charge on the nucleus is positive.

Definition of Terms:

atomic number (Z): number of protons in the nucleus
 for a neutral atom, ("neutral" means the atom has no charge)
 the # protons = # electrons so that total charge = 0
 the atomic number (# protons) determines an element's identity

Excerpts from Encyclopedia Britannica

Early Atomic Models

Several models of the atom were proposed in the first few years of the 20th century. The earliest (1902) was originated by an English physicist, Lord Kelvin, but was supported so strongly by Thomson that it became known as the Thomson atom. According to this model, the atom consists of a sphere of uniformly distributed positive charge, about one angstrom in diameter ($1 \text{ angstrom} = 10^{-10} \text{ m}$), in which the electrons are embedded like raisins in a pudding. Lord Kelvin himself at least partly abandoned this model and in 1905 proposed another, in which the uniform positive sphere is replaced by alternate positive and negative spherical shells, with a net surplus of positive charge; the electrons are embedded in the positive charge. Another model, proposed in 1903, suggested that all atoms are composed of varying numbers of a single constituent, called dynamids. Each dynamid is conceived as consisting of an intimate association of an electron and a much more massive positive body, having a linear dimension (diameter) of the order of 10^{-4} angstroms with the dynamids held together by unspecified forces. Still another model, proposed in 1904 by a Japanese physicist, Hantaro Nagaoka, considered the positive charge as concentrated at the center of the atom, with the electrons forming a ring similar to Saturn's rings.

The Rutherford Model

In 1910, two researchers working under Rutherford's direction, were studying the scattering of alpha particles - that is, their deflection from straight-line paths - as they passed through thin foils. They noted that a small but significant number were scattered through quite large angles. Rutherford recognized that, if the Thomson model were valid, an alpha particle, about 7000 times more massive than an electron, would interact with many atoms on the way through the foil; no single interaction could produce a large deflection, and the effects of the many interactions would tend to cancel rather than add up. On the other hand, if the positive charge and most of the mass were concentrated in a very small region at the center, as Nagaoka had suggested, multiple interactions would be rare, but a single interaction could produce a large deviation. Rutherford worked out the theory in 1911, that the atom could be described as a tiny, dense, positively charged core called a nucleus, in which nearly all the mass is concentrated, around which the light, negative constituents, called electrons, circulate at some distance, much like planets revolving around the Sun. He showed that the scattering should be proportional to the foil thickness, t , for a nuclear atom but to the square root of the thickness, \sqrt{t} , for the Thomson atom; that it should decrease with increasing deflection angle for a nuclear atom but decrease much faster for the Thomson atom. With refined techniques, a complete verification was obtained of the results of the nuclear model, based totally on classical physics. This model did have serious defects: the dynamic equilibrium he proposed, with the electrons travelling around the nucleus, meant, according electromagnetic theory, that the electrons would radiate energy continuously, lose energy and spiral into the nucleus. This does not happen. This problem was resolved by a Danish physicist, Niels Bohr, in 1913, with the Bohr model of the atom.

mass number (A): sum of numbers of protons and neutrons in the nucleus
 therefore, $A = Z + \text{no. of neutrons}$ (mass number is not atomic weight)

nuclide symbol

${}^A_Z E$ where E = element symbol
 A = mass number ($\#p + \#n$)
 Z = atomic number ($\#p$)

example: For ${}^{63}\text{Cu}$, what is number of protons, electrons, neutrons in atom

ANS. $\#p = 29$ (look on periodic table)
 $\#e = 29$ ($\#p = \#e$ for a neutral atom)
 $\#n = A - Z = 63 - 29 = 34$

isotopes: two or more forms of atoms of the same element with different masses; atoms containing the same number of protons, but different numbers of neutrons.

example: the element hydrogen has 3 isotopes:

hydrogen	deuterium	tritium
${}^1_1\text{H}$	${}^2_1\text{H}$	${}^3_1\text{H}$
(99.985%)	(0.015%)	(0.000%)
1 proton	1 proton	1 proton
1 electron	1 electron	1 electron
0 neutrons	1 neutron	2 neutrons

Some elements have only 1 isotope (F, I), but most elements occur in nature as mixtures of isotopes. The naturally occurring abundances of isotopes (Table 5-3) are determined by mass spectrometry

Atomic Weight Scale: $1 \text{ amu} = \frac{1}{12}$ mass of $^{12}_6\text{C}$, a specific isotope of C
where amu = atomic mass unit

recall: mass of one $^{12}_6\text{C}$ atom = 12 amu

mass of one mole of $^{12}_6\text{C}$ atoms = 12.0000 g

Atomic Weight of an element: weighted average of masses of its constituent isotopes.

Example: Copper occurs naturally as 2 isotopes

	% abundance	isotopic mass
^{63}Cu	69.1 %	62.9 amu
^{65}Cu	30.9 %	64.9

What is the atomic weight of copper?

$$\begin{aligned} \text{AW of Cu} &= (\text{fraction of } ^{63}\text{Cu})(\text{mass of } ^{63}\text{Cu}) + (\text{fraction of } ^{65}\text{Cu})(\text{mass of } ^{65}\text{Cu}) \\ &= (0.691)(62.9 \text{ amu}) + (0.309)(64.9 \text{ amu}) \\ &= 63.5 \text{ amu} \end{aligned}$$

Example: The atomic weight of boron is 10.811 amu. (or look up on periodic table)
The masses of the two isotopes are ^{10}B 10.013 amu, ^{11}B = 11.009 amu
What are the % abundances of the 2 isotopes?

let x = fraction of the lighter isotope, ^{10}B
 $1-x$ = fraction of the heavier isotope, ^{11}B

$$\begin{aligned} \text{AW of B} &= (\text{fraction of } ^{10}\text{B})(\text{mass of } ^{10}\text{B}) + (\text{fraction of } ^{11}\text{B})(\text{mass of } ^{11}\text{B}) \\ 10.811 &= (x)(10.013 \text{ amu}) + (1-x)(11.009 \text{ amu}) \\ 10.811 &= 10.013x + 11.009 - 11.009x \\ -0.198 &= -0.996x \\ x &= 0.199 \\ 1-x &= 0.801 \end{aligned}$$

\therefore % abundance of ^{10}B = 19.9 %
 ^{11}B = 80.1 %

Atoms and the Mole:

Recall $1 \text{ amu} = \frac{1}{12}$ mass of ^{12}C atom - was an arbitrary decision by scientists

From periodic table

$1.0079 \text{ amu} =$ mass of an average H atom (weighted average by mass)

$22.98977 \text{ amu} =$ mass of an average Na atom

therefore $\rightarrow \therefore$ a Na atom has ~ 23 times more mass than a H atom.

Now, atoms are very small, difficult to weigh, difficult to count
So, how do we measure them accurately?

We need a unit which describes a large number of atoms:

mole (SI units) $\text{mol} \equiv 6.022045 \times 10^{23}$ particles
Avogadro's number (N_A)

1 mol Na atoms has 6.022×10^{23} atoms of Na.
(show samples of moles - Fig 2.9)

The system of atomic weights was worked out with N_A so that
for an element, atomic weight (in amu) \equiv mass of 1 mol (in grams)
If you look on the periodic table for atomic weight (molar mass) of Na:
you will find 22.98977 or 22.99 (to 4 sig. figures)
 \therefore if you have 1 atom of Na, it has mass of 22.99 amu
if you have 1 mol of Na atoms, it has mass of 22.99 g.
Pretty amazing!

What about the units?

AW has units of $\frac{\text{grams}}{\text{mol}}$ or $\frac{\text{amu}}{\text{atom}}$
(molar mass)

So let's use the units as a formula!

Example: What is the identity of an element if 3.00 moles of it weighs 80.9 g?

Plan: mol, g \rightarrow A.W. \rightarrow use periodic table to find identity

atomic weight has units of $\frac{g}{mol}$ - use this as a formula!

$$\begin{aligned} \text{A.W.} \left(\frac{g}{mol} \right) &= \frac{\#g}{\# \text{ moles}} \\ &= \frac{80.9 g}{3.00 mol} \\ &= 27.0 \end{aligned}$$

\therefore element must be aluminum, Al

Example: Calculate the mass of an atom of Fe

From periodic table: 1 mol of Fe has mass of 55.85 g
we know 1 mol of Fe contains 6.022×10^{23} atoms

If we combine this information,

$$\text{mass of 1 Fe atom} = 55.85 \frac{g}{mol} \times \left(\frac{1 \text{ mol}}{6.022 \times 10^{23} \text{ atoms}} \right) = 9.274 \times 10^{-23} \frac{g}{\text{atom}}$$

(g/atom) UNIT FACTOR

Note: this is example of dimensional analysis.

Example: How many moles of atoms and how many atoms are contained in 26.2 g of Fe? (show sample)

$$(a) \text{ A.W.} \left(\frac{g}{mol} \right) = \frac{\#g}{\# mol} \Rightarrow \# \text{ moles} = \frac{\#g}{\text{AW}} \quad \text{This is a formula!!}$$

$$\begin{aligned} \therefore \# \text{ moles Fe} &= \frac{\#g \text{ Fe}}{\text{AW}} \\ &= \frac{26.2 g}{55.85 g/mol} \\ &= 0.469 \text{ mol} \end{aligned}$$

(b) likewise, we know N_A has units: $\frac{\text{particles}}{\text{mole}} \therefore N_A = \frac{\# \text{ particles}}{\# \text{ moles}}$

$$\begin{aligned} \therefore \# \text{ atoms} &= N_A \times \# \text{ moles} \\ &= 6.022 \times 10^{23} \frac{\text{atoms}}{\text{mol}} \times 0.469 \text{ mol} \\ &= 2.82 \times 10^{23} \text{ atoms} \end{aligned}$$

Example: How many moles of Hg and how many atoms of Hg are contained in 9.84 mL of Hg (Show vial). Specific gravity of Hg = 13.5939.

we know that $\# \text{ moles} = \frac{\# \text{ g}}{\text{AW}}$ but we do not know mass, only volume.
What do we know that relates mass and volume? ANS. DENSITY (specific gravity)

$$\begin{aligned} \text{density has units } \frac{\text{g}}{\text{mL}} \text{ (or } \frac{\text{g}}{\text{cm}^3}) & \therefore D = \frac{\# \text{ g}}{\# \text{ mL}} \\ \# \text{ g} &= D \times \# \text{ mL} \end{aligned}$$

\therefore the units of density give you the formula for relating D , mL, g

Recall: specific gravity: ratio of the density of a substance to the density of H_2O (= 1.00 g/mL at 25°C to 3 significant fig)
 \therefore for all practical purposes, density \equiv specific gravity
($\frac{\text{g}}{\text{mL}}$) (no units)

Back to the example:

Plan of attack: $\text{mL} \xrightarrow[\text{or Sp.gr.}]{(1) D} \text{g} \xrightarrow{\text{AW}} (2) \text{ moles} \xrightarrow{N_A} (3) \text{ atoms}$

$$\begin{aligned} (1) \# \text{ g Hg} &= D \times \# \text{ mL} && \text{since } D = \frac{\# \text{ g}}{\# \text{ mL}} \\ &= 13.5939 \frac{\text{g}}{\text{mL}} \times 9.84 \text{ mL} \\ &= 134 \text{ g} \end{aligned}$$

$$(2) \# \text{ mol Hg} = \frac{\# \text{ g}}{\text{AW}} = \frac{134 \text{ g}}{200.59 \frac{\text{g}}{\text{mol}}} = 0.668 \text{ mol} \quad \text{since } \text{AW} = \frac{\# \text{ g}}{\# \text{ mol}}$$

$$\begin{aligned} (3) \# \text{ atoms} &= \# \text{ moles} \times N_A \\ &= 0.668 \text{ mol} \times 6.02 \times 10^{23} \frac{\text{atom}}{\text{mol}} = 4.02 \times 10^{23} \text{ atoms} \end{aligned} \quad \text{since } N_A = \frac{\# \text{ atoms}}{\# \text{ mol}}$$

Same problem by dimensional analysis:

$$\begin{aligned} \# \text{ atoms Hg} &= 9.84 \text{ mL Hg} \times \frac{13.5939 \text{ g}}{1 \text{ mL}} \times \frac{1 \text{ mol}}{200.59 \text{ g}} \times \frac{6.02 \times 10^{23} \text{ atoms Hg}}{1 \text{ mol Hg}} \\ &= 4.02 \times 10^{23} \text{ atoms Hg} \end{aligned}$$

In dimensional analysis, each step is represented by a unit factor

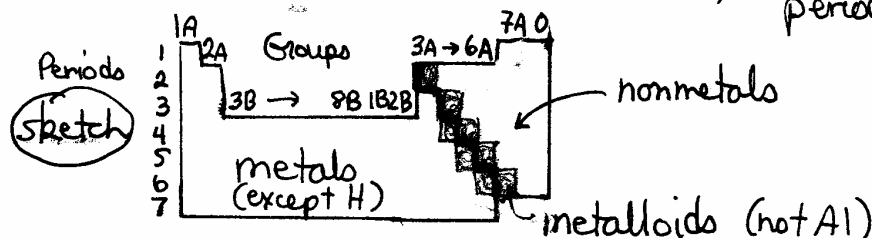
Step 1: converting mL \rightarrow g

Step 2: converting g \rightarrow mol

Step 3: converting mol \rightarrow atoms

Introduction to Periodic Table

- the properties of the elements are periodic functions of their atomic number.
(atomic # is # protons in nucleus - and # electrons in a neutral atom)
- Groups or families: vertical columns
 - 1A (except H): alkali metals
 - 2A: alkaline earths
 - 7A: halogens (salt formers)
 - 8A (0): noble gases - used to be called inert
- Periods: horizontal rows. First row is Period 1.
- Elements can be divided into 3 classes (by staircase division on periodic table).



- characteristics:

metals

1. high electrical conductivity
2. all are solids (ex. Hg) at room T
3. form cations (+ charged ions)
by losing electrons
4. form ionic compounds with nonmetals

nonmetals

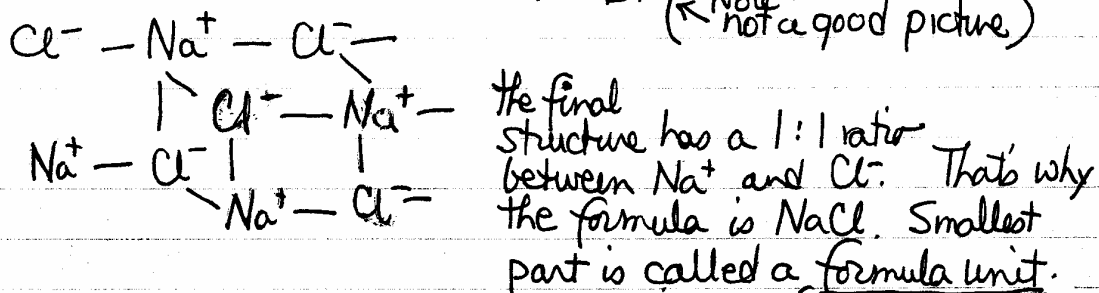
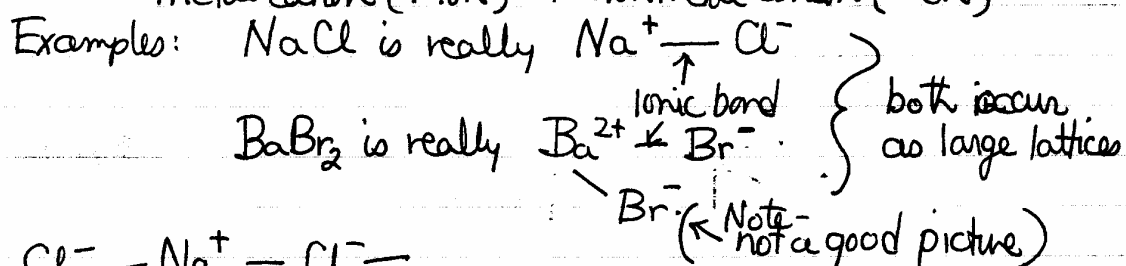
1. poor electrical conductivity
2. gases, liquids or solids ^{at room}
3. form anions (- charged ions)
by gaining electrons
4. forms covalent compounds with other non-metals.

(OLD CHAPTER 3 - NOW A PART OF CHAPTER 2)

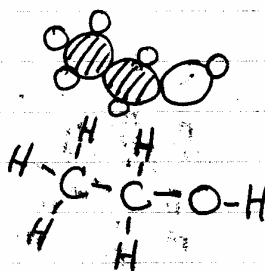
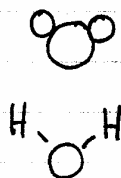
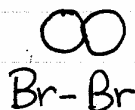
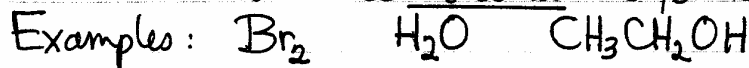
How do atoms attach themselves to other atoms and how do we name these new compounds?

Two main ways are used to form compounds:

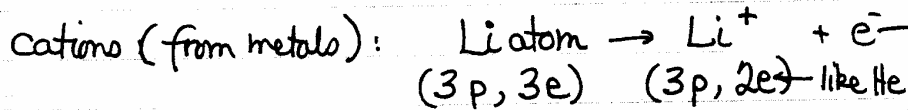
(1) electrons are transferred from one atom to another to form ions. Ions are held together by electrostatic forces, called ionic bonds. You easily recognize ionic compounds because they are a metal cation (+ ion) + nonmetal anion (- ion).



(2) electrons are shared between atoms. No ions are formed. Atoms are held together by forces called covalent bonds. Covalent compounds are easily recognized because they occur between nonmetals. On the smallest level, the individual units called molecules are formed.

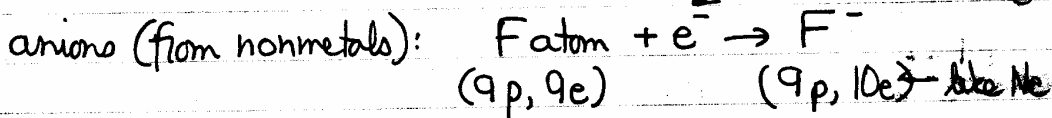


More on ions and ion formation:

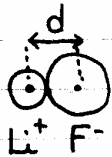


The electron is transferred from the Li atom to F atom and LiF is made

Note: elements want to have same #e⁻ as noble gases for stability. (more later)



the force of attraction, the electrostatic force, called ionic bond is set by Coulomb's Law



$$F \propto \frac{(n^+ \cdot e)(n^- \cdot e)}{d^2}$$

is proportional to

n = charge on + or - ion
 e = charge on electron
 d = distance between ions
 F = force

Introduction to Nomenclature for Ionic Compounds:

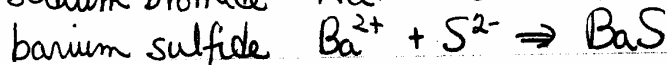
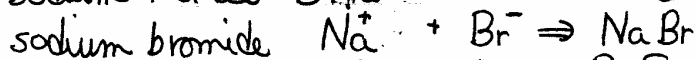
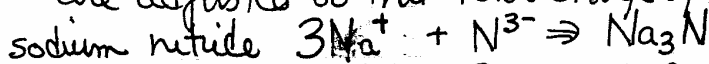
common cations:	Na^+ sodium ion	Cl^- chloride ion
	K^+ potassium ion	Br^- bromide ion
	Ba^{2+} barium ion	S^{2-} sulfide ion
	Al^{3+} aluminum ion	N^{3-} nitride ion

Note: for simple 2 element (binary) ionic compounds only:

1A +1	2A +2	3A +3	metals
5A -3	6A -2	7A -1	nonmetals

name: cation name + anion name - very simple.

formula: you must know charges on ions! Relative numbers of ions are adjusted so that total charge of compound is \emptyset .



Naming Compounds

This is definitely IMPORTANT!

I Binary compounds : composed of 2 elements
 can be ionic or covalent
 name less electronegative element first and the more
 electronegative element second with -ide ending on its stem.

Stems for Nonmetals

IIIA	IVA	VA	VIA	VIIA
B bor	C carb	N nitr	O ox	H hydr
	Si silic	P phosph	S sulf	F fluor
		As arsen	Se selen	Cl chlor
		Sb antimon	Te tellur	Br brom
				I iod

A Binary ionic compounds : contain metal cations and nonmetal anions

KBr : potassium bromide

Mg₃P₂ : magnesium phosphide

CaCl₂ : calcium chloride

Al₂O₃ : aluminum oxide

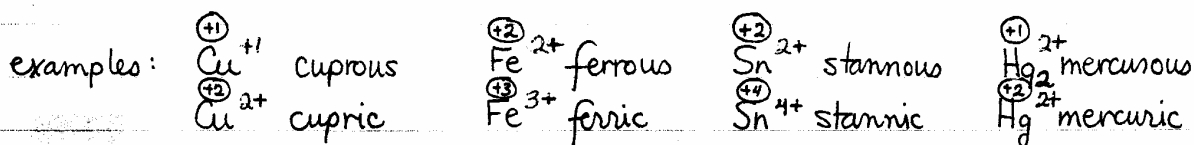
NaH : sodium hydride (H is more electronegative - it is anion with -1 charge

EN 1.0 2.1

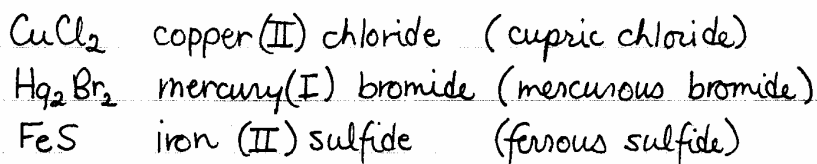
Metals in binary compounds may exhibit more than one oxidation number.
 There are 2 ways to express this information.

(1) older method : "-ous" ending for lower oxidation state
 "-ic" ending for higher oxidation state

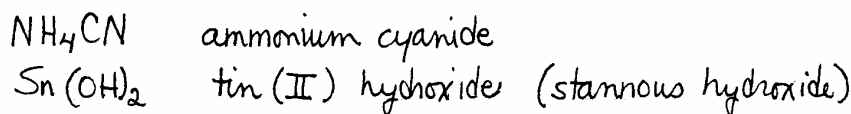
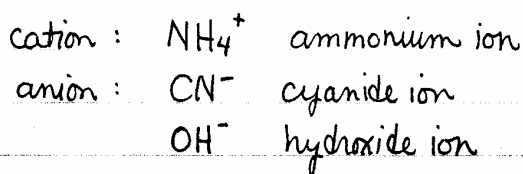
• This only works for those metals with 2 different oxidation numbers.



(2) IUPAC method : use roman numeral in parentheses following name



B. Pseudobinary ionic compounds: contain more than 2 elements

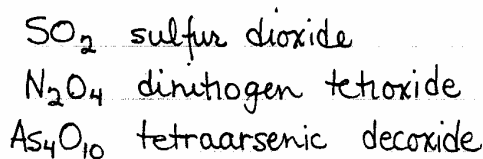


C. Binary Covalent compounds : contains 2 nonmetals

Greek/Latin prefixes give elemental proportions

- | | | | |
|--------------------|----------|----------|------------|
| 1. mono (trivial*) | 4. tetra | 7. hepta | 10. deca |
| 2. di | 5. penta | 8. octa | 11. undeca |
| 3. tri | 6. hexa | 9. nona | 12. dodeca |

* except for carbon monoxide, CO



D. Binary acids : H + more electronegative nonmetal

HCl (g)	hydrogen chloride	HCl (aq)	hydrochloric acid
HF (g)	hydrogen fluoride	HF (aq)	hydrofluoric acid
HI (g)	hydrogen iodide	HI (aq)	hydroiodic acid
HCN (g)	hydrogen cyanide	HCN (aq)	hydrocyanic acid
H ₂ S (g)	hydrogen sulfide	H ₂ S (aq)	hydrosulfuric acid

II Ternary Compounds

A. Ternary acids (oxyacids) : compounds of H, O, nonmetal

Common ternary acids : "-ic" acids

III A	IV A	V A	VI A	VII A
$\overset{+3}{\text{H}_3\text{BO}_3}$ boric acid	$\overset{+4}{\text{H}_2\text{CO}_3}$ carbonic acid	$\overset{+5}{\text{HNO}_3}$ nitric acid		
	$\overset{+4}{\text{H}_4\text{SiO}_4}$ silicic acid	$\overset{+5}{\text{H}_3\text{PO}_4}$ phosphoric acid	$\overset{+6}{\text{H}_2\text{SO}_4}$ sulfuric acid	$\overset{+5}{\text{HClO}_3}$ chloric acid
		$\overset{+5}{\text{H}_3\text{AsO}_4}$ arsenic acid	$\overset{+6}{\text{H}_2\text{SeO}_4}$ selenic acid	$\overset{+5}{\text{HBrO}_3}$ bromic acid
			$\overset{+6}{\text{H}_6\text{TeO}_6}$ telluric acid	$\overset{+5}{\text{HIO}_3}$ iodic acid

There are sets of acids derived from the -ic ternary acids :

- 1 more O : per___ic acid
- 1 less O : ___ous acid
- 2 less O : hypo___ous acid

oxidation state (number) of nonmetal increases ↑

per___ic acid
___ic acid
___ous acid
hypo___ous acid

perchloric acid
chloric acid
chlorous acid
hypochlorous acid

HClO₄
HClO₃
HClO₂
HClO

oxidation no. of Cl

+7
+5
+3
+1

B. Ternary Salts: cation (+) or NH_4^+ (ammonium ion) goes first
anion (-) derived from acid goes second

-ic acid \Rightarrow -ate ion per___ic acid \Rightarrow per___ate ion
-ous acid \Rightarrow -ite ion hypo___ous acid \Rightarrow hypo___ite ion

HIO_4	periodic acid	$\xrightarrow{-\text{H}^+}$	IO_4^-	periodate ion
HIO_3	iodic acid	$\xrightarrow{-\text{H}^+}$	IO_3^-	iodate ion
HIO_2	iodous acid	$\xrightarrow{-\text{H}^+}$	IO_2^-	iodite ion
HIO	hypiodous acid	$\xrightarrow{-\text{H}^+}$	IO^-	hypiodite ion

Note: the charge on the ion can be deduced from the number of Hydrogens on the parent acid.

H_3PO_4	phosphoric acid	$\xrightarrow{-3\text{H}^+}$	PO_4^{3-}	phosphate ion
HNO_2	nitrous acid	$\xrightarrow{-1\text{H}^+}$	NO_2^-	nitrite ion
H_2SO_4	sulfuric acid	$\xrightarrow{-2\text{H}^+}$	SO_4^{2-}	sulfate ion
H_2SO_3	sulfurous acid	$\xrightarrow{-2\text{H}^+}$	SO_3^{2-}	sulfite ion
H_2CO_3	carbonic acid	$\xrightarrow{-2\text{H}^+}$	CO_3^{2-}	carbonate ion

Examples of salts:

ammonium sulfate	$(\text{NH}_4)_2\text{SO}_4$
calcium nitrite	$\text{Ca}(\text{NO}_2)_2$
iron(II) phosphate (ferrous phosphate)	$\text{Fe}_3(\text{PO}_4)_2$

C. Acid Salts: salts containing an acidic hydrogen or two.

	IUPAC	older name
NaHSO_4	sodium hydrogen sulfate	sodium bisulfate
NaHSO_3	sodium hydrogen sulfite	sodium bisulfite
KH_2PO_4	potassium dihydrogen phosphate	—
NaHCO_3	sodium hydrogen carbonate	sodium bicarbonate

Here is a list of common ions - memorize!

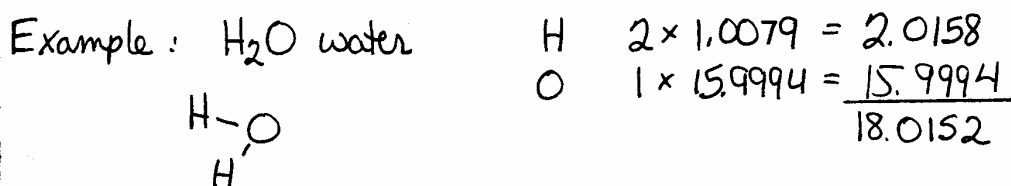
Formulas and Names for Some Common Ions

Common Cations		Common Anions	
Formula	Name	Formula	Name
Li ⁺	lithium ion	F ⁻	fluoride ion
Na ⁺	sodium ion	Cl ⁻	chloride ion
K ⁺	potassium ion	Br ⁻	bromide ion
NH ₄ ⁺	ammonium ion	I ⁻	iodide ion
Ag ⁺	silver ion	OH ⁻	hydroxide ion
Mg ²⁺	magnesium ion	CN ⁻	cyanide ion
Ca ²⁺	calcium ion	ClO ⁻	hypochlorite ion
Ba ²⁺	barium ion	ClO ₂ ⁻	chlorite ion
Cd ²⁺	cadmium ion	ClO ₃ ⁻	chlorate ion
Zn ²⁺	zinc ion	ClO ₄ ⁻	perchlorate ion
Cu ²⁺	copper(II) ion or cupric ion	* CH ₃ COO ⁻	acetate ion
Hg ₂ ²⁺	mercury(I) ion or mercurous ion	* MnO ₄ ⁻	permanganate ion
Hg ²⁺	mercury(II) ion or mercuric ion	NO ₂ ⁻	nitrite ion
Mn ²⁺	manganese(II) ion	NO ₃ ⁻	nitrate ion
Co ²⁺	cobalt(II) ion	* SCN ⁻	thiocyanate ion
Ni ²⁺	nickel(II) ion	O ²⁻	oxide ion
Pb ²⁺	lead(II) ion or plumbous ion	S ²⁻	sulfide ion
Sn ²⁺	tin(II) ion or stannous ion	HSO ₃ ⁻	hydrogen sulfite ion or bisulfite ion
Fe ²⁺	iron(II) ion or ferrous ion	SO ₃ ²⁻	sulfite ion
Fe ³⁺	iron(III) ion or ferric ion	HSO ₄ ⁻	hydrogen sulfate ion or bisulfate ion
Al ³⁺	aluminum ion	SO ₄ ²⁻	sulfate ion
Cr ³⁺	chromium(III) ion or chromic ion	HCO ₃ ⁻	hydrogen carbonate ion or bicarbonate ion
		CO ₃ ²⁻	carbonate ion
		* CrO ₄ ²⁻	chromate ion
		* Cr ₂ O ₇ ²⁻	dichromate ion
		PO ₄ ³⁻	phosphate ion
		AsO ₄ ³⁻	arsenate ion

* additional ions that you come across

Formulas, Compounds & The Mole

Formula weight: sum of masses of elements in the formula.
(FW)



H_2O is made of nonmetals, so it is a covalent compound.
The smallest part of H_2O that still has H_2O characteristics is the molecule.

∴ one tiny little molecule of H_2O "weighs" 18.0152 amu and FW = 18.0152 amu/molecule. has a mass of

and if you have 1 mole ($N_A = 6.02 \times 10^{23}$ molecules) of H_2O , it would "weigh" 18.0152 grams.
The FW = 18.0152 g/mol of H_2O molecules.

since the density of water ~ 1.00 g/mL (depends on T) you would have ~ 18 mL of H_2O .

Note: since water is a molecule, FW can also be molecular wt.

Example: How many molecules of H_2O are in 100. mL of H_2O ?
Plan: mL H_2O $\xrightarrow{(1)}$ g H_2O $\xrightarrow{(2)}$ mol H_2O $\xrightarrow{(3)}$ molecules H_2O

we know

$$(1) D \left(\frac{\text{g}}{\text{mL}} \right) = \frac{\# \text{g}}{\# \text{mL}} \quad \therefore \# \text{g} = D \times \# \text{mL} = 1.00 \text{ g/mL} \times 100. \text{ mL} = 100. \text{ g}$$

$$(2) \text{MW} (\text{g/mol}) = \frac{\# \text{g}}{\# \text{mol}} \quad \therefore \# \text{mol} = \frac{\# \text{g}}{\text{MW}} = \frac{100. \text{ g}}{18.0 \text{ g/mol}} = 5.56 \text{ mol } \text{H}_2\text{O}$$

$$(3) N_A = \frac{\# \text{particles}}{\# \text{mol}} \quad \therefore \# \text{molecules} = N_A \times \# \text{mol} = 6.02 \times 10^{23} \frac{\text{molecules}}{\text{mol}} \times 5.56 \text{ mol} = 3.35 \times 10^{24} \text{ molecules } \text{H}_2\text{O}$$

OR

$$\# \text{molecules } \text{H}_2\text{O} = 100 \text{ mL } \text{H}_2\text{O} \times \frac{1.00 \text{ g}}{1.00 \text{ mL}} \times \frac{1 \text{ mol } \text{H}_2\text{O}}{18.0 \text{ g } \text{H}_2\text{O}} \times \frac{6.02 \times 10^{23} \text{ molecules } \text{H}_2\text{O}}{1 \text{ mole } \text{H}_2\text{O}}$$

Example: Calculate formula weight of $\text{Al}_2(\text{SO}_4)_3 \cdot 18 \text{H}_2\text{O}$

aluminum sulfate: $\text{Al}_2(\text{SO}_4)_3$

hydrated aluminum sulfate: $\text{Al}_2(\text{SO}_4)_3 \cdot 18 \text{H}_2\text{O}$

anhydrous
(no waters attached)
hydrate

Al	exact 2	inexact 26.98	=	53.96
S	3	32.06	=	96.18
O	³⁰ (12 + 18)	16.00	=	480.0
H	36	1.008	=	<u>36.29</u>
				666.47 g /mole formula weight

∴ if we have 1 mole of this compound, what do we really have?

$$\begin{aligned}
 1 \text{ mole } \text{Al}_2(\text{SO}_4)_3 \cdot 18 \text{H}_2\text{O} &\equiv 6.022 \times 10^{23} \text{ formula units} \\
 (666.4 \text{ g}) &\equiv 2 \text{ moles of Al } (53.96 \text{ g}) \\
 &\equiv 2 \times 6.022 \times 10^{23} \text{ atoms of Al} \\
 &\equiv 3 \text{ moles of S } (96.18 \text{ g}) \\
 &\equiv 30 \text{ moles of O} \\
 &\equiv 18 \text{ moles of H}_2\text{O } (18 \times 18.0 = 324 \text{ g H}_2\text{O})
 \end{aligned}$$

Percent Composition and Formulas of Compounds

percent composition: percent by mass of each element in the compound.

Example: Calculate the percent by mass of the elements in $\text{Al}_2(\text{SO}_4)_3 \cdot 18 \text{H}_2\text{O}$

Assume: you have 1 mole of compound $\equiv 666.4 \text{ g}$ in this case (see above)

$$\% \text{ Al} = \frac{\text{mass of Al in formula unit}}{\text{formula weight}} \times 100 = \frac{53.96}{666.4} \times 100 = 8.097 \%$$

$$\% \text{ S} = \frac{\text{mass of S in formula unit}}{\text{formula weight}} \times 100 = \frac{96.18}{666.4} \times 100 = 14.43 \%$$

$$\% \text{ O} = \frac{\text{mass of O}}{\text{F.W.}} \times 100 = \frac{480.0}{666.4} \times 100 = 72.03 \%$$

$$\% \text{ H} = \frac{\text{mass of H}}{\text{F.W.}} \times 100 = \frac{36.29}{666.4} \times 100 = \frac{5.446 \%}{100.007 \%}$$

All samples of hydrated aluminum sulfate have this composition.
(Law of Definite Proportions)

Law of Multiple Proportions: If two elements combine to form more than one compound, the ratio of the masses can be expressed in small whole numbers

e.g. H, O H_2O H_2O_2 $\therefore \frac{\text{mass of O in H}_2\text{O}}{\text{mass of O in H}_2\text{O}_2} = \frac{1}{2}$
 water hydrogen peroxide

Derivation of Formulas from Elemental Composition

Many times in the laboratory, a chemist will synthesize a compound. To help prove that she prepared what she thought she prepared, she will send a sample of the new compound to a commercial laboratory for elemental analysis. From this information, she can deduce the simplest or empirical formula (the smallest whole number ratio of atoms present in a compound).

Examples of simplest (empirical) formulas:

TRUE MOLECULAR FORMULA

C_6H_6 (benzene)

As_4O_{10}

SO_2

SIMPLEST FORMULA

CH

As_2O_5

SO_2

Example: Consider a compound that only contains carbon and hydrogen. The results come back: 85.6% C and 14.4% H. What is the simplest (empirical) formula for the compound?

Step ①: Assume we have 100 g of compound - to make calculations easier.
 \therefore we have 85.6 g C and 14.4 g H.

Step ②: Recall that formulas involve ratios of atoms or moles of atoms
NOT mass.

\therefore we must change mass of element \rightarrow moles of element.

$$\# \text{ moles C} = \frac{85.6 \text{ g C}}{12.0 \text{ g/mol}} = 7.13 \text{ moles C} \quad \text{since mol} = \frac{g}{\text{AW}}$$

$$\# \text{ moles H} = \frac{14.4 \text{ g H}}{1.00 \text{ g/mol}} = 14.4 \text{ moles H}$$

Recall that the elements in a formula are in a ratio of whole numbers to each other.

Step ③ Choose the smallest number of moles to use as a divisor for the other numbers.

$$\text{for C} \quad \frac{7.13}{7.13} = 1.00$$

But the ratios must be whole numbers.

$$\text{for H} \quad \frac{14.4}{7.13} = 2.02$$

$$\therefore \frac{\text{mol C}}{\text{mol H}} = \frac{1}{2}$$

\therefore empirical formula for the compound is CH_2

To continue, the chemist knows from another experiment that the molecular weight of her compound is 42. What is the true or actual formula?

The simplest formula, CH_2 , has as its formula weight

$$\text{C: } 1 \times 12.011 = 12.011$$

$$\text{H: } 2 \times 1.008 = \underline{2.016}$$

$$14.027 \text{ amu}$$

But,

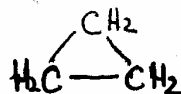
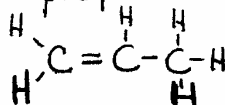
$$\text{actual formula weight} = \text{empirical formula weight} \times \text{whole number}$$

$$42 = 14x$$

$$x = 3$$

$$\therefore \text{actual formula} = (\text{CH}_2)_3 = \text{C}_3\text{H}_6$$

So, sample could be propene or cyclopropane.



Example: What is the simplest formula for a compound: 65.20% As, 34.80% O ?

	① Assume 100 g	② change to moles	③ divide by smallest #
As	65.20 g	$\rightarrow \frac{65.20 \text{ g}}{74.92 \text{ g/mol}} = 0.8703$	$\frac{0.8703}{0.8703} = 1.000$
O	34.80 g	$\rightarrow \frac{34.80 \text{ g}}{16.00 \text{ g/mol}} = 2.175$	$\frac{2.175}{0.8703} = 2.499$

Now, you have found the formula $\text{As}_1\text{O}_{2.499}$

What do you do to change subscripts to whole numbers ?

You do NOT round off ! to give either AsO_2 or AsO_3

You DO multiply thru by 2 to give As_2O_5 .

Note: only round off when < 0.1 or so from whole number.

e.g. $\text{FeO}_{1.33}$ does not round off to FeO . Multiply by 3 to give Fe_3O_4 .

Additional Problem:

How many atoms of Oxygen are contained in a 9.80g sample of H_2SO_4 ? (MW $\text{H}_2\text{SO}_4 = 98.0 \text{ g/mol}$)

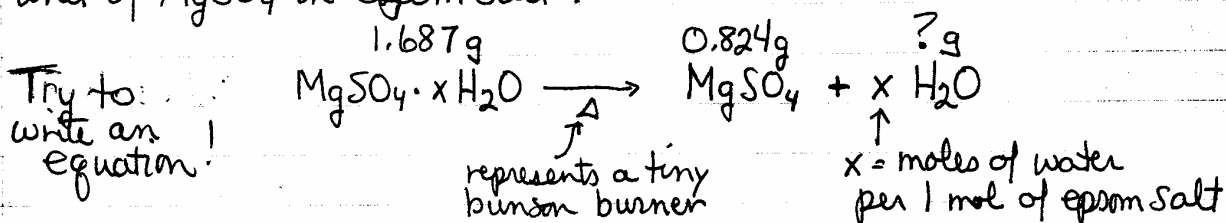
Plan: $\text{g H}_2\text{SO}_4 \xrightarrow{(1)} \text{moles H}_2\text{SO}_4 \xrightarrow[\text{or}]{(2) \text{ either}} \text{moles O} \xrightarrow{(3)} \text{atoms O}$
 $\text{molecules H}_2\text{SO}_4 \rightarrow \text{atoms O}$

$$(1) \text{ moles H}_2\text{SO}_4 = \frac{9.80 \text{ g}}{98.0 \text{ g/mol}} = 0.100 \text{ moles H}_2\text{SO}_4$$

$$(2) \text{ moles O} = 4 \times \text{moles H}_2\text{SO}_4 = 0.400 \text{ moles O} \quad \text{since } \frac{4 \text{ moles O}}{1 \text{ mol H}_2\text{SO}_4}$$

$$(3) \text{ atoms O} = 6.02 \times 10^{23} \frac{\text{atoms}}{\text{mole}} \times 0.400 \text{ moles} = \underline{2.41 \times 10^{23} \text{ atoms O}}$$

#57. If Epsom salt, $\text{MgSO}_4 \cdot x \text{H}_2\text{O}$ is heated to 250°C , all the water of hydration is lost. On heating 1.687 g sample of the hydrate, 0.824 g of MgSO_4 remains. How many molecules of water occur per formula unit of MgSO_4 in epsom salt?



Law of conservation of matter says that in any ordinary process or reaction (not a nuclear reaction),
mass of reactants = mass of products

You can easily see that the mass of water in the epsom salt sample must be $1.687 - 0.824 = 0.863 \text{ g H}_2\text{O}$

Since formulas deal with ratios of moles, not grams, we must convert!

$$\# \text{ moles MgSO}_4 = \frac{0.824 \text{ g}}{120.4 \text{ g/mol}} = 0.00684 \text{ mol}$$

$$\# \text{ moles H}_2\text{O} = \frac{0.860 \text{ g}}{18.0 \text{ g/mol}} = 0.0478 \text{ mol}$$

if we divide, we know how many moles of H_2O per mole of MgSO_4 which is the same ratio as the number of molecules of H_2O per formula unit of MgSO_4 .

$$\frac{\# \text{ moles of H}_2\text{O}}{\# \text{ moles MgSO}_4} = \frac{0.0478 \text{ mol H}_2\text{O}}{0.00684 \text{ mol MgSO}_4} = 6.99 \text{ or } 7$$

since it must be a whole number

\therefore formula of epsom salt must be: $\text{MgSO}_4 \cdot 7 \text{H}_2\text{O}$