

## Chapter 13: Liquids and Solids

In our study of gases, we related the physical properties of gases to the behavior of the molecules that make up the gas through the KINETIC-MOLECULAR THEORY.

We are now going to do a similar comparison between physical properties and molecule behavior for liquids and solids. Then we will look at the changes that occur when a substance changes phase ie  $\text{gas} \rightleftharpoons \text{liquid} \rightleftharpoons \text{solid}$ .

There are 3 states of matter:  $\begin{matrix} & \text{gas} & \text{liquid} & \text{solid} \\ & \searrow & \downarrow & \swarrow \\ \text{fluid} & & \text{condensed: particles are} \\ & & \text{in close contact with each other} \end{matrix}$

If we could look at molecules:

MORE ORDERED  
increase in intermolecular attraction  $\longrightarrow$

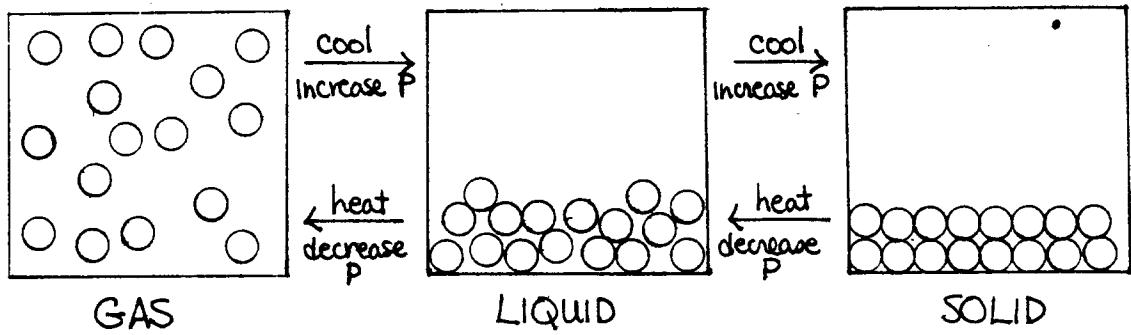


Fig 13-1

- |                    |                          |                        |
|--------------------|--------------------------|------------------------|
| 1. no shape        | 1. no shape              | 1. definite shape      |
| 2. compressible    | 2. not very compressible | 2. not compressible    |
| 3. low density     | 3. medium density        | 3. high density        |
| 4. diffuse rapidly | 4. diffuse thru liquids  | 4. very slow diffusion |
| 5. disordered      | 5. disordered            | 5. ordered             |

Effect of pressure: think of P as forcing the molecules together.

Effect of temperature: As T decreases, kinetic energy of molecules decrease until forces of attraction between molecules overcomes KE  $\Rightarrow$  liquification but there is still some disorder.

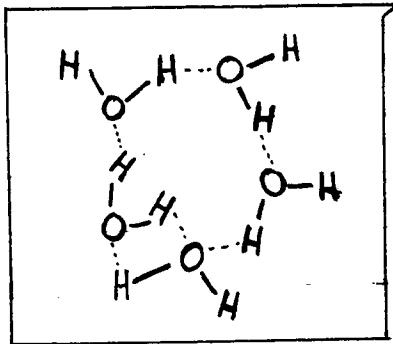
As T continues to decrease, there are stronger forces of attraction

which cause ordering to occur and at low enough temperatures, the liquid solidifies or freezes.

But what are these intermolecular forces in gases and liquids?

First, let's illustrate what we are discussing.

Consider a beaker of water (illustration of hydrogen bonding)  $\text{H}_2\text{O} = \text{H}-\ddot{\text{O}}-\text{H}$



... intermolecular forces are forces between individual particles

- intramolecular forces are within each molecule  
These are strong covalent bonds that bind the atoms together in molecule.

Intermolecular forces operate over short distances. If not for these forces, the condensed phases (liquids & solids) would not exist; gases would never change to liquids and solids.

### Kinds of Intermolecular Forces in Liquids

1. ion-ion interaction : molten salts ( $\text{NaCl}$ ,  $\text{MgBr}_2$ ,  $\text{KClO}_4$  etc in molten state)

very strong interaction

force of attraction between 2 oppositely charged ions - governed by

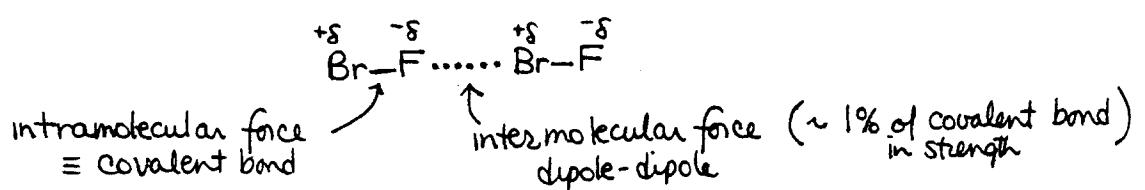
Coulomb's Law:  $F \propto \frac{q^+ q^-}{d^2}$  where  $q^+$  charge on cation  
 $q^-$  charge on anion  
 $d$  distance between them

characteristics of molten salts:

- (1) have high boiling points because ion-ion interaction is strong
- (2) ionic substances with multiple charges ( $\text{Al}^{3+}$ ,  $\text{Mg}^{2+}$ ,  $\text{O}^{2-}$ ,  $\text{S}^{2-}$ ) have higher B.P. than those with singly charged ions ( $\text{Cl}^-$ ,  $\text{Na}^+$ , etc) due to Coulomb's Law.
- (3) conduct electricity well since ions are mobile.

2. Dipole-dipole interactions: polar covalent molecules ( $\text{CHCl}_3$ ,  $\text{BrF}$ ,  $\text{SO}_2$ )  
 medium strength interaction - less strong than ion-ion attraction  
 force of attraction between  $+\delta$  end of one molecule and  $-\delta$  end of another:

$\begin{array}{c} +\delta \\ \text{Br} - \text{F} \\ \text{EN} \quad 2.8 \quad 4.0 \end{array}$	$\begin{array}{l} +\delta \text{ small positive charge} \\ -\delta \text{ small negative charge} \end{array}$
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characteristics of liquids of polar covalent molecules

- (1) Boiling points are lower than for molten salts since dipole-dipole interactions are weaker than ion-ion interactions.
- (2)  $\therefore$  these liquids are more volatile.

3. Hydrogen bonding: polar covalent molecules composed of H bonded to a small highly EN. atom such as O, N, F  
 special case of dipole-dipole interactions  
 stronger interaction than dipole-dipole interactions.  
 force of attraction between  $+\delta$  end of molecule (H) and  $-\delta$  end of another (small, highly electronegative element such as O, F, N).

examples:  $\text{HF}$ ,  $\text{H}_2\text{O}$ ,  $\text{NH}_3$ ,  $\text{CH}_3\text{OH}$ ,  $\text{CH}_3\text{COOH}$



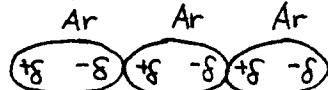
characteristics

- (1) strength of H bond may be as high as 10% of covalent bond
- (2) compounds having H bonding have anomalously high boiling points.

4. London forces: non-polar covalent molecules ( $\text{Ne}$ ,  $\text{CO}_2$ ,  $\text{Cl}_2$ ,  $\text{CH}_4$ )  
 (also named Van der Waals attraction, dispersion forces, dipole-induced dipole attractive forces that exist over very short distances ( $F \propto \frac{1}{d^7}$ ))

E.g.  $\text{Ar}$   $\rightarrow$    
 non-polar temporary dipole but at any instant, a non-polar molecule is a temporary dipole

a temporary dipole can induce a dipole in other atoms.



more polarizable

### Characteristics

- (think of water balloons) (1) the larger the molecule, the easier it becomes to induce dipoles since the electron cloud is larger and more easily distorted.
- ∴ London forces are more important in larger molecules (molecules with higher MW's) and are oftentimes more important in determining physical properties of liquids than permanent dipole-dipole interactions.

Example: Table 13-3 H-Cl      permanent dipole-dipole energy 3.3 kJ/mol  
London energy 17.8 kJ/mol

Let's consider some examples to illustrate these intermolecular forces:

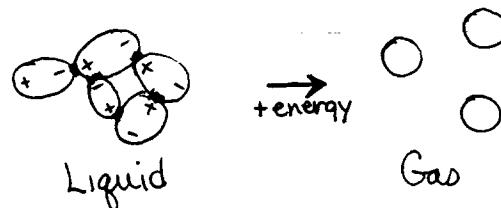
Consider the boiling points of the noble gases as a function of molecular size:

Noble Gas	Molecular Weight*	BP (°C)
He	4	-268.9
Ne	20	-246.0
Ar	40	-185.7
Kr	84	-152.3
Xe	131	-107.1
Rn	222	-61.8

\* as a measure of size

The increase in b.p. as function of molecular size can be interpreted as it becoming more and more difficult to break the intermolecular forces between molecules in the liquid to form isolated molecule in the gas. ∴ more + more energy is required to do this as molecules get larger.

The intermolecular forces in this case are London Forces.



Another series of nonpolar molecules are the hydrocarbons. Boiling point increases due to increasing London forces.

Formula	Name	Structure	Molecular wt.	B.P.(°C)
CH <sub>4</sub>	methane	-C-	16	-164
C <sub>2</sub> H <sub>6</sub>	ethane	-C-C-	30	-88.6
C <sub>3</sub> H <sub>8</sub>	propane	-C-C-C-	44	-42.1
n-C <sub>4</sub> H <sub>10</sub>	normal butane	-C-C-C-C-	58	-0.5
n-C <sub>5</sub> H <sub>12</sub>	normal pentane	-C-C-C-C-C-	72	36.1

The following is more complicated: the hydrides of IVA, VA, VIA and VIIA elements

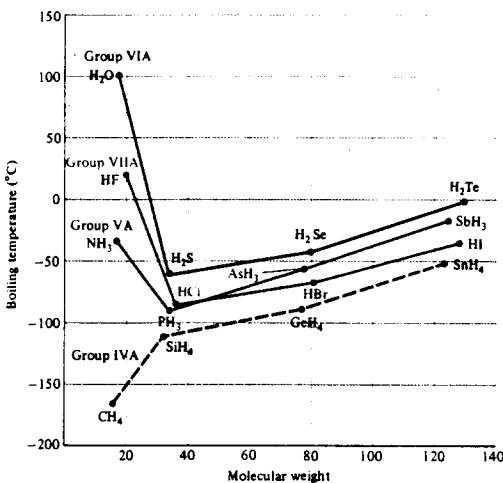


FIGURE 13-5 Boiling points of some hydrides as a function of molecular weight. The anomalously high boiling points of NH<sub>3</sub>, H<sub>2</sub>O, and HF compared with those of other hydrides of the same groups are due to hydrogen bonding. The electronegativity difference between H and C is small and there are no lone pairs on C; thus, CH<sub>4</sub> is not hydrogen bonded.

Group IVA hydrides : CH<sub>4</sub> < SiH<sub>4</sub> < GeH<sub>4</sub> < SnH<sub>4</sub> in size ; these are nonpolar.

- London forces are operating and become stronger as molecules get larger.
- B.P. increases as molecular weight increases.

Group VA hydrides : NH<sub>3</sub> < PH<sub>3</sub> < AsH<sub>3</sub> < SbH<sub>3</sub> in size

- these are polar  $\begin{array}{c} \text{H} \quad \text{N}^{\delta-} \\ | \quad || \\ \text{H} \quad \text{H}^{\delta+} \end{array}$  and dipole-dipole interactions are expected.

These should decrease as MW  $\uparrow$  since  $\Delta\text{EN}$  between VA element and H decrease. The result : BP  $\downarrow$  as MW  $\uparrow$ . This is not seen.

- B.P. increases since size of molecule increases and London forces increase
- The higher B.P. for NH<sub>3</sub> is due to H-bonding.

Group VIA and VIIA hydrides : same trend as VA : high B.P. due to H-bonding.

HF and H<sub>2</sub>O have anomalously

To summarize,

- (1) without intermolecular forces, liquids and solids would not exist.
- (2) these forces affect physical properties of liquids
- (3) the relative strengths of the forces are as follows:

London forces ~ dipole-dipole interactions < hydrogen bonding < ion-ion interaction

Example: Arrange the following substances in order of increasing boiling point



lowest BP	$\text{Ne}$	$<$	$\text{C}_2\text{H}_6$	$<$	$\text{AsH}_3$	$<$	$\text{NH}_3$	$<$	$\text{NaCl}$	$<$	$\text{MgO}$
monatomic molecule (small)	nonpolar covalent molecule (larger)		polar covalent molecule		polar covalent molecule (even larger)				ionic		ionic
Forces: London	London		London		London		London		ion-ion		ion-ion
			dipole-dipole		H-bonding						
											(contains ions with greater charge)
											$F \propto \frac{q_1 q_2}{d^2}$

Note: all covalent compounds have London dispersion forces.

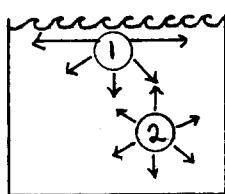
### The Liquid State - Properties (depend on intermolecular forces)

(1) viscosity : a measure of the resistance to flow

e.g. molasses in January (sugar has much H-bonding) has higher viscosity than gasoline ( $\text{C}_8\text{H}_{18}$ )

depends on intermolecular forces, size and shape of molecules  
is a function of temperature: as  $T \uparrow$ , intermolecular forces  $\downarrow$ , viscosity  $\downarrow$

(2) surface tension : a measure of inward forces that must be overcome to expand the surface area of liquid. Surface tension is what allows bugs to "walk" on water and water drops to be spheres.

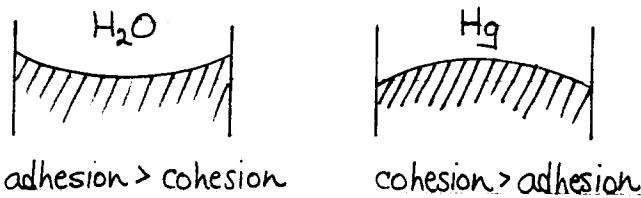


particle 2 is equally attracted to all its neighbors  
particle 1 at the surface is NOT completely surrounded by neighbors and holds more tightly to the ones it has.

(3) capillary action: the process by which a liquid may climb a small diameter tube (e.g. roots of plants)

the result of adhesive forces (force of attraction between the liquid and another surface) being greater than cohesive intermolecular forces (forces holding the liquid together)

consider the meniscus:



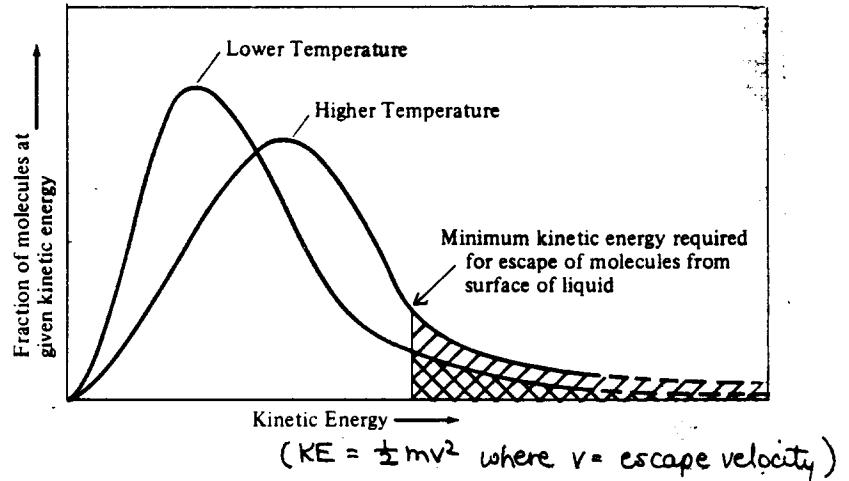
### Evaporation, Vapor Pressure and Boiling Point of Liquids

What is involved when a liquid changes to a gas?

Evaporation: the process by which molecules break away from the surface of a liquid and become a gas

molecules need a minimum amount of kinetic energy ( $\propto$  absolute T) in order to do this.

FIGURE 13-10 Distribution of kinetic energies of molecules in a liquid at different temperatures. At the lower temperature, a smaller fraction of the molecules has the energy required to escape from the liquid, so evaporation is slower at the lower temperature.

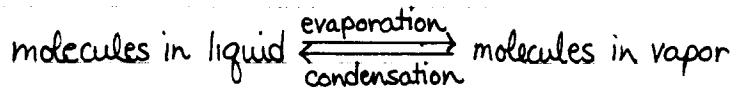
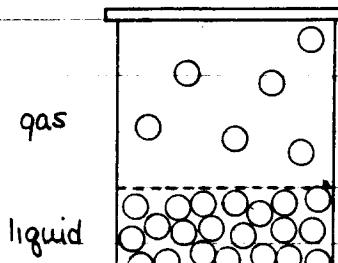


When the temperature is higher, there is a greater fraction of molecules with the necessary kinetic energy to escape from the liquid.

$\therefore$  the rate of evaporation is higher at higher temperatures.. (sensible)

the reverse process is called condensation.

In a closed container, a dynamic equilibrium is set up after a period of time.



at equilibrium, the rate at which molecules in liquid become molecules in gas (vapor) is equal to the rate at which gaseous molecules become liquid.

If the top of the beaker were removed, the system could NOT reach equilibrium and the water would evaporate as the system tries to reach equilibrium. (An illustration of Le Chatelier's principle - a system at equilibrium will react to undo any stress put on the system.)

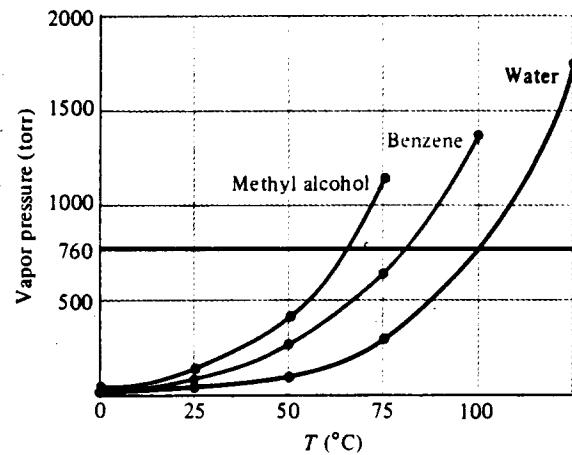
Vapor Pressure : partial pressure of vapor above the surface of the liquid  
AT EQUILIBRIUM with the vapor.

- as temperature increases, the vapor pressure increases.
- vapor pressures of different liquids are different due to their having different intermolecular forces.
- in general, liquids with strong intermolecular forces (molten salts, H<sub>2</sub>O etc) have low vapor pressures and high boiling points.

Boiling Point : the temperature at which the vapor pressure of the liquid equals the applied pressure - usually atmospheric pressure.

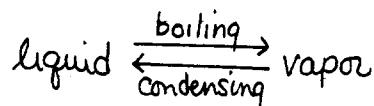
∴ at the boiling point, vapor pressure = applied pressure

at this temperature, bubbles of vapor form beneath the surface of the liquid and rise to the surface. In other words, evaporation occurs **EVERYWHERE** in the liquid, not just at the surface.



These are plots of vapor pressure of some liquids vs temperature. The NORMAL boiling point of these liquids occurs at the temperature where their vapor pressure equals 1 atm (760 torr) (Figure 13-13)

at the boiling point, the liquid and vapor exist in equilibrium.



Since different liquids have different intermolecular attractions, they have different vapor pressures and different boiling points at the same applied pressure.

It is possible to separate a mixture of liquids into its components by exploiting their different boiling points. This process is called DISTILLATION.

The liquid with the lowest boiling point is separated out first (Fig 13-14)

### The Solid State - An Introduction

Just as the intermolecular forces in liquids (ion-ion, dipole-dipole, hydrogen-bonding, London) must be broken for the liquid to become a gas, the intermolecular forces existing in solids (more later) must be overcome for a solid to become a liquid.

Melting Point (Freezing Point): the temperature at which liquid and solid exist together at equilibrium

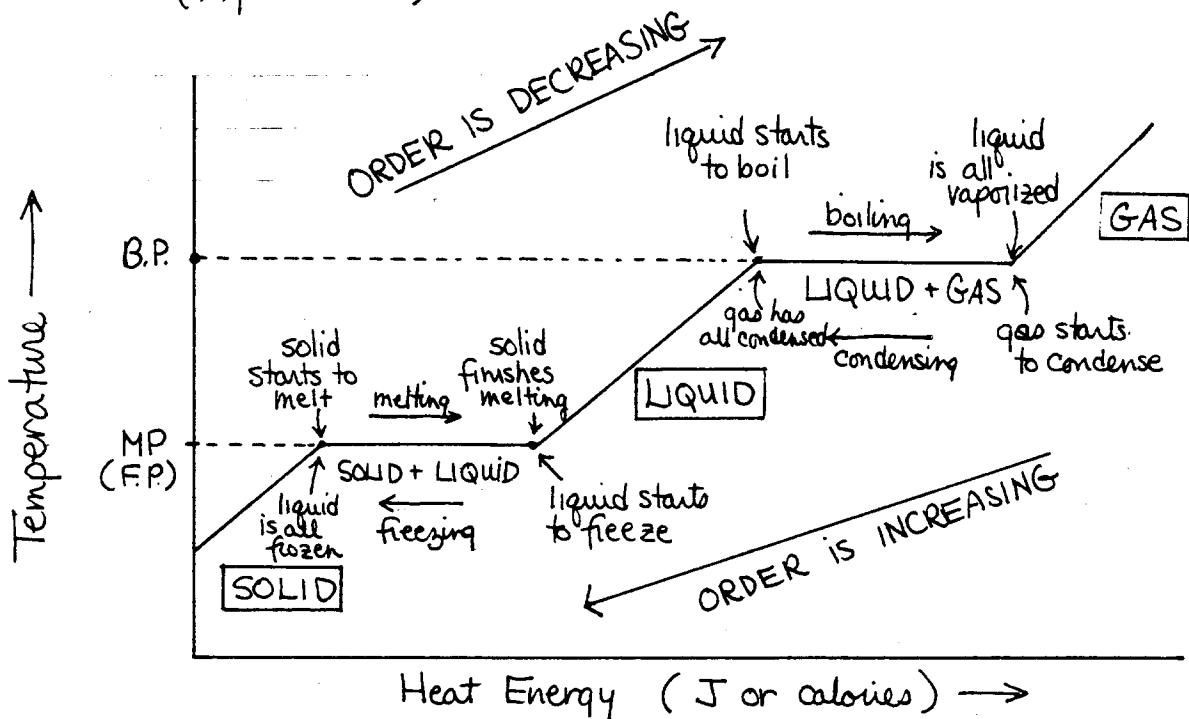
At the melting point, solid  $\xrightleftharpoons[\text{freezes}]{\text{melts}}$  liquid dynamic equilibrium

the normal melting point is the melting point at 1 atm pressure.

How do we break the intermolecular forces holding solids and liquids together?

ANS. We add heat!!!

(Figure 13-15)



Heat is absorbed by system as solid → liquid → gas.

This process of breaking intermolecular forces is ENDOOTHERMIC.

Heat is released by system as gas → liquid → solid

This process is EXOTHERMIC.

The amount of heat absorbed or released by a system during phase changes can be accurately calculated.

### Terminology:

Joule and calorie are units of heat. 1 calorie = 4.184 J

Specific heat of a substance in a certain phase (gas, liquid, solid)

is the amount of heat required to raise the temperature of 1 g of the substance by  $1^{\circ}\text{C}$ . with no change in state.

Specific heat has units of ( $\text{J/g}^{\circ}\text{C}$ ). Heat = Sp. H.  $\times$  mass  $\times \Delta T$

Heat of fusion: the amount of heat required to melt 1 g of a solid at its melting point. Units: ( $\text{J/g}$ ). It is also the amount of heat released when 1 g of a liquid freezes at its freezing point.

Amount of Heat = heat of fusion  $\times$  mass

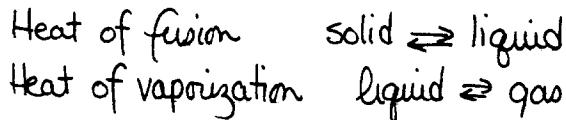
ExtraDifference Between Specific Heat ( $\frac{J}{g \cdot ^\circ C}$ ) and Heat of Fusion/Vaporization ( $\frac{J}{g}$ )

Specific heat is a constant particular to a certain substance in a specific phase which relates how much heat in joules is necessary to change the temperature of a certain amount of the substance (without changing its phase).

Example: If 15.0 g of iron(s) cools from 35.0°C to 9.0°C, thereby releasing 173 J of heat, what is the specific heat of iron(s)?

$$\text{Specific heat } \left( \frac{J}{g \cdot ^\circ C} \right) = \frac{\text{heat (J)}}{\text{mass(g)} \times \Delta T(^{\circ}C)} = \frac{173 \text{ J}}{15.0 \text{ g} \times (35.0 - 9.0)^{\circ}C} = 0.444 \text{ J/g}^{\circ}C$$

Heat of Fusion/Vaporization ( $J/g$ ) is a constant particular to a certain substance that is changing phase at the temperature where the phase change occurs:



occurs at freezing/melting pt  
occurs at boiling point

The constant relates how much heat is necessary for the phase change to occur at the phase change temperature for a certain mass of compound.

Example: If 327 J of heat are removed from 3.00 g of  $\text{CH}_3\text{CH}_2\text{OH}(l)$  at  $-117^{\circ}\text{C}$ , what is the heat of fusion of ethanol? The freezing point of ethanol is  $-117^{\circ}\text{C}$ .

$$\text{Heat of Fusion } \left( \frac{J}{g} \right) = \frac{\text{heat (J)}}{\text{mass (g)}} = \frac{327 \text{ J}}{3.00 \text{ g}} = 109 \text{ J/g}$$

Note: temperature or temperature change is not involved for heat of fusion or heat of vaporization because the process is occurring at the phase change temperature.

**Heat of vaporization :** the amount of heat required to vaporize 1 g of a liquid to a gas at its boiling point. Units : (J/g). It is also the amount of heat released when 1 g of vapor condenses to 1 g of liquid at the boiling point. Amount of heat = heat of vap. × mass

Example: How many joules of energy must be absorbed by 500 g of H<sub>2</sub>O at 50°C to convert it to 500 g of steam at 120°C?

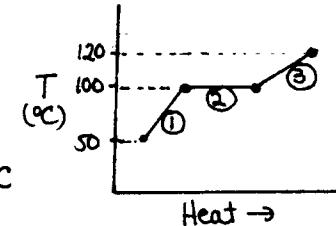
Given : Specific heat H<sub>2</sub>O(l) : 4.18 J/g°C

Specific heat H<sub>2</sub>O(g) : 2.03 J/g°C

Heat of vaporization H<sub>2</sub>O :  $2.26 \times 10^3$  J/g

B.P. H<sub>2</sub>O : 100°C

liquid      ① → liquid      ② → gas      ③ → gas  
50°C                  100°C                  100°C                  120°C



where ① heat needed to raise T of 500g H<sub>2</sub>O to its B.P. at 100°C

② heat needed to change all water into steam at 100°C

③ heat needed to raise T of steam from 100°C to 120°C

$$\text{Total Heat Absorbed} = ① + ② + ③$$

$$= [\text{Sp. H. H}_2\text{O}(l) \times \text{mass H}_2\text{O} \times \Delta T] + [\text{H. of vap.} \times \text{mass H}_2\text{O}] \\ + [\text{Sp. H. of H}_2\text{O}(g) \times \text{mass H}_2\text{O} \times \Delta T]$$

$$= [4.18 \frac{\text{J}}{\text{g°C}} \times 500\text{g} \times (100-50\text{°C})] + [2.26 \times 10^3 \frac{\text{J}}{\text{g}} \times 500\text{g}] \\ + [2.03 \frac{\text{J}}{\text{g°C}} \times 500\text{g} \times (120-100\text{°C})]$$

$$= 104 \text{ kJ} + 1130 \text{ kJ} + 20 \text{ kJ}$$

$$= 1250 \text{ kJ}$$

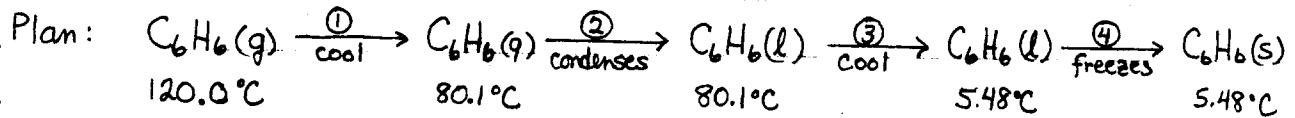
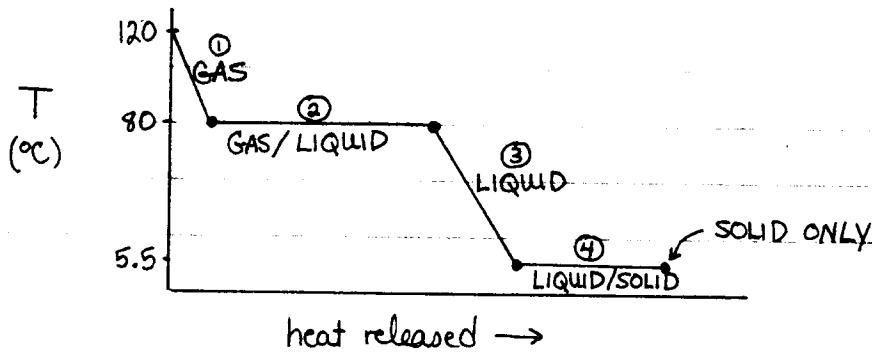
$$= 1.25 \times 10^6 \text{ J}$$

Note that the energy required to break the intermolecular bonds in liquid water is very high due primarily to hydrogen bonding.

Example: How much heat (in kJ) must be removed when cooling 155 g of benzene,  $C_6H_6$ , at  $120.0^\circ C$  to solid benzene at  $5.48^\circ C$ ?

Given for benzene: b.p. at 1 atm:  $80.1^\circ C$   
m.p. at 1 atm:  $5.48^\circ C$

specific heat ( $\lambda$ ):  $1.74 \text{ J/g}^\circ C$   
specific heat ( $g$ ):  $1.04 \text{ J/g}^\circ C$   
heat of fusion:  $127 \text{ J/g}$   
heat of vaporization:  $395 \text{ J/g}$



$$\text{Total heat released} = \text{①} + \text{②} + \text{③} + \text{④}$$

$$\text{① heat}_{\text{released}} = \text{Sp. Ht}(g) \times \text{mass} \times \Delta T = 1.04 \text{ J/g}^\circ C \times 155 \text{ g} \times (120.0 - 80.1)^\circ C = 6.43 \text{ kJ}$$

$$\text{② heat}_{\text{released}} = \text{Ht vap.} \times \text{mass} = 395 \text{ J/g} \times 155 \text{ g} = 61.2 \text{ kJ}$$

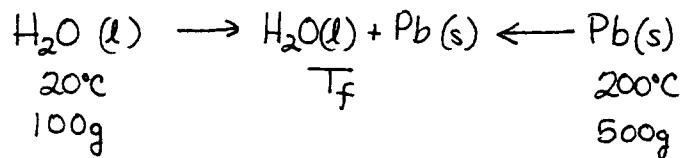
$$\text{③ heat}_{\text{released}} = \text{Sp. Ht}(\lambda) \times \text{mass} \times \Delta T = 1.74 \text{ J/g}^\circ C \times 155 \text{ g} \times (80.1 - 5.48)^\circ C = 20.1 \text{ kJ}$$

$$\text{④ heat}_{\text{released}} = \text{Ht fusion} \times \text{mass} = 127 \text{ J/g} \times 155 \text{ g} = 19.7 \text{ kJ}$$

$$\therefore \text{total heat released} = \text{①} + \text{②} + \text{③} + \text{④} = 107.4 \text{ kJ}$$

Example: If 500g of lead at 200°C are placed in 100g of water at 20°C in an insulated container, what will be the temperature when the lead and water are at the same temperature?

Given: Specific heat of H<sub>2</sub>O (l) : 4.18  $\frac{\text{J}}{\text{g} \cdot \text{C}}$   
 Specific heat of Pb(s) : 0.159  $\frac{\text{J}}{\text{g} \cdot \text{C}}$



heat gained by water = heat lost by Pb

$$4.18 \frac{\text{J}}{\text{g} \cdot \text{C}} \times 100\text{g} \times (T_f - 20) = 0.159 \frac{\text{J}}{\text{g} \cdot \text{C}} \times 500\text{g} \times (200 - T_f)$$

$$418 T_f - 8360 \text{ J} = 15900 \text{ J} - 79.5 T_f$$

$$498 T_f = 24260 \text{ J}$$

$$T_f = 48.7 \text{ }^\circ\text{C}$$

When substances at different temperatures are mixed, heat is transferred from the warmer substance to the cooler substance and the final temperature of the mixture is intermediate between the original temperatures of the substances.

Example: If 5000 J of heat are removed from 500g of H<sub>2</sub>O (l) at 62°C what will be its final temperature?

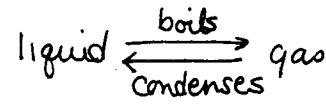
$$5000 \text{ J} = 4.18 \frac{\text{J}}{\text{g} \cdot \text{C}} \times 500\text{g} \times (62 - T_f)$$

$$5000 \text{ J} = 130,000 \text{ J} - 2090 T_f$$

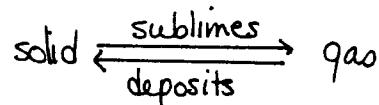
$$2090 T_f = 125000 \text{ J}$$

$$T_f = 59.8 \text{ }^\circ\text{C}$$

In these calculations we have used the following equilibrium situations



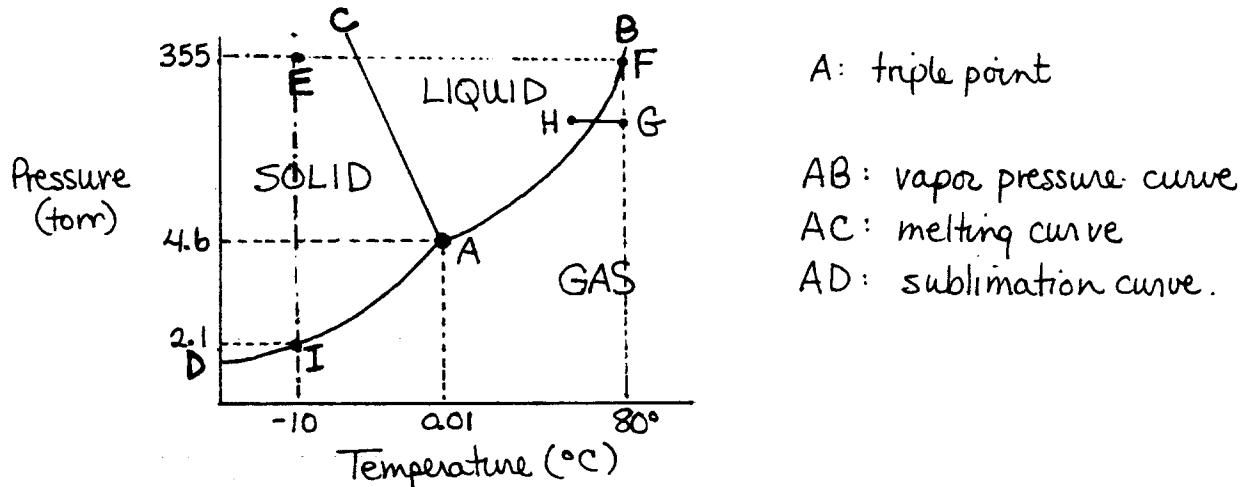
Some solids (iodine, dry ice:  $\text{CO}_2(s)$ ) change directly to a gas at atm. pressure.



All these changes of one phase to another are dependent on both  $T + P$ .

One useful way of summarizing all this data regarding phase transitions for any pure substance is the PHASE DIAGRAM, which gives pressure-temperature relationships for all phases at equilibrium.

Consider the phase diagram for  $\text{H}_2\text{O}$  (not to scale)



A: triple point

AB: vapor pressure curve

AC: melting curve

AD: sublimation curve.

A is called the TRIPLE POINT. At 4.6 torr and  $0.01^{\circ}\text{C}$ ,  $\text{H}_2\text{O}$  exists at equilibrium as a solid, liquid and gas. From this point we draw the lines AB defines the P-T boundary where  $\text{liquid} \rightleftharpoons \text{gas}$   
 AC defines the P-T boundary where  $\text{solid} \rightleftharpoons \text{liquid}$   
 AD defines the P-T boundary where  $\text{solid} \rightleftharpoons \text{gas}$

From the phase diagram:

- (1)  $\text{H}_2\text{O}$  cannot exist as a liquid if  $P < 4.6$  torr
- (2) Point E at 355 torr and  $-10^{\circ}\text{C}$  shows  $\text{H}_2\text{O}$  to be a solid  
 If the  $T \uparrow$  as  $P$  constant, to point F, the solid will melt at the intersection of AC to a liquid and will start to boil at Point F

∴ at point F we have equilibrium liquid  $\rightleftharpoons$  gas at 355 tor, 80°C  
 If the temperature is held constant and pressure is decreased, H<sub>2</sub>O vapor exists solely as a gas. (Point G). If temperature is decreased to 70°C (Point H) the gas condenses to a liquid.

Starting at Point E, and decreasing the pressure to Point I on the sublimation curve keeping the temperature at T = -10°C, we have solid  $\rightleftharpoons$  gas at equilibrium at 2.1 tor + -10°C.  
 If the pressure is reduced further, the solid sublimes to a gas (process is called freeze-drying).

### The Solid State Revisited:

Solids can be defined as being

(1) amorphous : no well-defined crystal structure, lacking internal regularity,  
 examples : rubber, some plastics, glass (also called supercooled liquid)

(2) crystalline : compact ordered arrangement of particles.

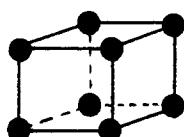
- X-ray diffraction - discussed in text - can determine the positions of atoms, ions, molecules in the structure.

All crystals are polyhedra having regularly repeating arrays of atoms, molecules or ions.

The smallest unit of volume of a crystal showing all the characteristics of its lattice is called the UNIT CELL. The unit cell fits into one of seven crystal systems (Table 13-9, p 482). There are 14 possible crystal lattices (Figure 13-22, p 483). A unit cell is the repeating unit in a crystal.

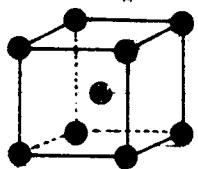
Let's discuss three simple unit cells: (For Interest Only)

(1) cubic



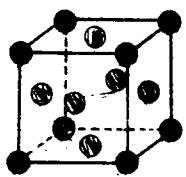
If all atoms are the same, how many atoms in the unit cell:  $8 \times \frac{1}{8} = 1$  atom/unit cell

## (2) body centered cubic

atoms in unit cell: corners  $8 \times \frac{1}{8} = 1$ center  $1 \times 1 = 1$ 

2 atoms/unit cell

## (3) face centered cubic

atoms in unit cell: corners  $8 \times \frac{1}{8} = 1$ faces  $6 \times \frac{1}{2} = 3$ 

4 atoms/unit cell

side view —○—

A crystal has the same geometry as the unit cell.

Isomorphous : different substances that crystallize in the same kind of lattice.

e.g. LiBr + NaCl crystallize in face centered cubic lattice.

polymorphous : a single substance that crystallizes in more than one form.

e.g. CaCO<sub>3</sub> : calcite (density : 2.710)

aragonite (density : 2.930)

For Interest Only:

Example: An unknown metal crystallizes in a body centered cubic lattice with a unit cell edge length of 3.301 Å ( $1 \text{ \AA} = 1 \times 10^{-8} \text{ cm}$ ). Its density is 8.569 g/cm<sup>3</sup> at 20°C. Identify the metal.

The unit cell of a body centered cubic lattice contains 2 atoms/unit cell. (see above)

$$\text{volume of unit cell} = (\text{edge length})^3 = (3.301 \times 10^{-8} \text{ cm})^3 = 35.97 \times 10^{-24} \text{ cm}^3.$$

$$\begin{aligned} \text{Density} &= \frac{\text{mass}}{\text{cm}^3} \quad \therefore \# \text{ atoms} = D \times \text{volume in cm}^3 = \text{mass of unit cell. (2 atoms)} \\ &= 8.569 \frac{\text{g}}{\text{cm}^3} \times 35.97 \times 10^{-24} \text{ cm}^3 \\ &= 3.082 \times 10^{-22} \text{ g / 2 atoms} \end{aligned}$$

$$\therefore 1 \text{ atom weighs } \frac{3.082 \times 10^{-22} \text{ g}}{2} = 1.541 \times 10^{-22} \text{ g}$$

$$1 \text{ mole of atoms weighs } 1.541 \times 10^{-22} \text{ g} \times 6.022 \times 10^{23} \frac{\text{atoms}}{\text{mole}} = 92.81 \frac{\text{g}}{\text{mole}}$$

$\therefore 92.81 \frac{\text{g}}{\text{mole}}$  is the molecular weight  $\therefore$  41Nb is the element

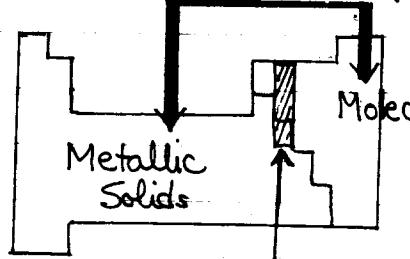
## Classification of Crystalline Solids

This is based on (1) types of particles making up the lattice  
 (2) types of bonding found in the lattice

Solids	Particles	Interparticle Forces	Properties	Examples
1. molecular	molecules or noblegases (atoms)	London, dipole-dipole H-bonding	soft poor conductors of heat, electricity low melting point	$\text{CH}_4$ , Ar $\text{PH}_3$ , $\text{NH}_3$ $\text{H}_2\text{O}$
2. covalent or network	atoms	covalent bonds (strong)	very hard poor conductor high melting point	C (diamond) C (graphite) $\text{SiO}_2$ (quartz)
3. ionic	cations & anions	electrostatic	hard, brittle poor conductor high melting point	$\text{NaCl}$ $\text{CaBr}_2$ & other salts
4. metallic	metal ions in a cloud of electrons	metallic bonds: (electrical attraction between cation and electrons)	soft $\rightarrow$ hard good conductors wide range of melting points	Li, K Ca, Cu and other metals

Using the periodic table to identify types of solids:

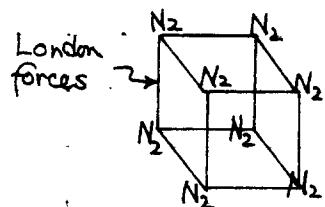
Ionic Solids (metal + nonmetal)



Covalent  
Solids (composed of some C, Si, Ge substances)

Melting Points for solids, like boiling points for liquids, give information about the strength of attractive forces between particles in solids : the higher the m.p. the stronger the interparticle forces in solids.

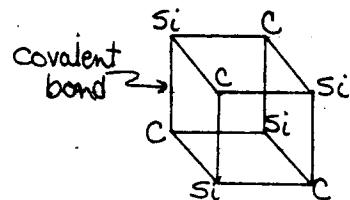
1. molecular solids : low melting points because the attractive forces between the molecules are weak: London, dipole-dipole, hydrogen bonding.



eg $\text{H}_2\text{O}$ (s)	m.p. $0^\circ\text{C}$
$\text{NH}_3$ (s)	m.p. $-77^\circ\text{C}$
$\text{N}_2$ (s)	m.p. $-209^\circ\text{C}$

$\text{N}_2$  crystallizes in cubic structure

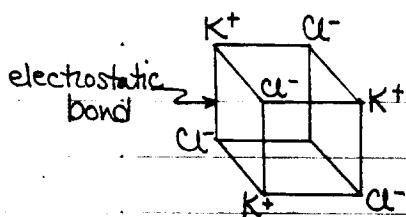
2. covalent solids : very high melting points since in order to melt the solid it is necessary to break covalent bonds.



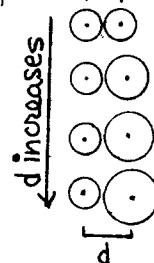
eg $\text{SiO}_2$ (s)	mp $1610^\circ\text{C}$
$\text{C}_{\text{diamond}}$ (s)	mp. $>3550^\circ\text{C}$
$\text{SiC}$ (s)	mp. $2700^\circ\text{C}$

cubic structure

3. ionic solids : high melting point due to electrostatic forces  $\frac{q^+q^-}{d}$

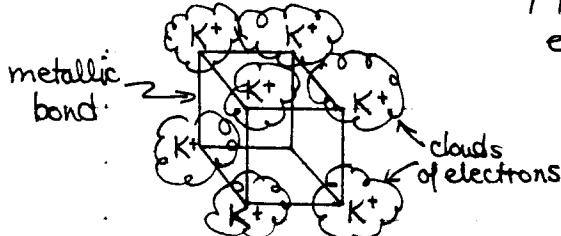


eg $\text{KF}$ (s)	mp $846^\circ\text{C}$
$\text{KCl}$ (s)	mp $776^\circ\text{C}$
$\text{KBr}$ (s)	mp $730^\circ\text{C}$
$\text{KI}$ (s)	mp $686^\circ\text{C}$



The halide ions increase in diameter,  $d$  increases  
Therefore, the electrostatic force decreases  $F \propto \frac{q^+q^-}{d^2}$

4. metallic solids : melting point is variable



eg $\text{K}$ (s)	mp $64^\circ\text{C}$
$\text{Pb}$ (s)	mp $327^\circ\text{C}$
$\text{Al}$ (s)	mp $660^\circ\text{C}$

Example: Identify the following crystalline solids:

Crystalline Solid	m.p.	Electrical Conductivity		Type
		Solid	Liquid	
C (graphite)	high	poor	poor	covalent
NaCl	high	no	yes	ionic
Na	high	yes	yes	metallic
O <sub>2</sub>	low	no	no	molecular

### Metallic Bonding and Band Theory

Most metals crystallize in close packed lattices.

∴ we know that the attractive interparticle forces are great.

Why is this? According to theories we have used, representative metals and d-transition metals do not have enough valence electrons to account for this.

A new theory was developed, Band Theory, which accounts for bonding and properties of metallic solids (Section 13-17). It explains the differences between conductors (metals), semi-conductors and insulators.

Metallic bonding is thought to result from the electrical attractions among positively charged metal ions and mobile, delocalized electrons belonging to the crystal as a whole.

Note: There is some confusion about differences between a molecular solid and a covalent solid. Consider  $\text{CO}_2$  and  $\text{SiO}_2$ . Both C and Si are IVA elements but

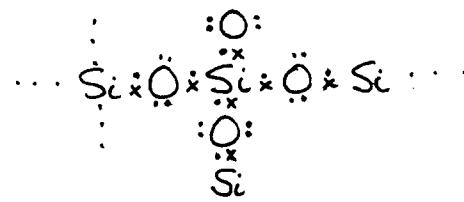
$\text{CO}_2$  forms a molecular solid m.p.  $-56.6^\circ\text{C}$  @ 5.2 atm.  
 $\text{SiO}_2$  forms a covalent solid m.p.  $1610^\circ\text{C}$   
 (quartz)

Why?

I  $\text{CO}_2$ : the Lewis dot structure is  $\ddot{\text{O}}\text{:}\text{C}:\ddot{\text{O}}$  or  $\text{:}\ddot{\text{O}}=\text{C}=\ddot{\text{O}}\text{:}$   
 it is a non polar molecule  
 $\therefore$  the only interparticle forces at work are London forces  
 which are very weak and very easily broken, hence low m.p.  
 as a solid, molecules are at the corners of the crystalline  
 lattice:  

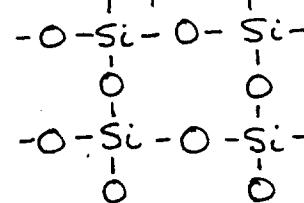
$$\begin{array}{c} \text{:}\ddot{\text{O}}_2\text{:} \quad \text{:}\ddot{\text{O}}_2\text{:} \\ | \qquad | \\ -\text{CO}_2-\text{CO}_2- \\ | \qquad | \\ -\text{CO}_2-\text{CO}_2- \end{array}$$

II  $\text{SiO}_2$  or  $(\text{SiO}_2)_n$ : since Si does not form double bonds, the Lewis structure is

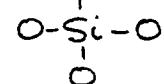


Note: Si does not form double bonds with oxygen, like its fellow IVA element C does, because of its larger size. The p orbitals on Si are just too far away from the p orbitals on oxygen to effectively overlap side-on to form a  $\pi$  bond.

and we have a solid in which all the atoms are covalently bonded together in a network.



each Si is the center of a tetrahedron:



if we count the atoms

Si : 4  
 O 8

and ratio gives  $\text{SiO}_2$